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RESEARCH ARTICLE

Analysis of Particle Swarm-Aided Power Plant Optimization

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#### Abstract

Stochastic optimization algorithms are usually evaluated based on performance on high dimensional benchmark functions and results of these tests determine the direction of development. Benchmark functions however, do not emulate complex engineering problems. In this paper a power plant optimization problem is presented and solved under different constraints with multiple elite dependent and single elite dependent swarm intelligence. Although on benchmark problems multiple elite dependent algorithms usually outperform single elite dependent ones, if search space is represented by simulation software, diversity not just increases iterations but computation time as well and because of that conventional PSO (particle swarm optimization) exceeds modified ones.

# Keywords

particle swarm optimization, power plant optimization, plant performance monitoring software, thermodynamic simulation

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# **1** Introduction

The increasing complexity of search space and growing number of variables, typical for engineering problems of our time have a great impact on optimization methods. Instead of traditional optimization techniques which have limited scope in practical applications heuristic search methods become more and more frequently used tools [1]. PSO can be considered one of the most important nature-inspired computing methods in optimization research [2]. It has several properties in common with other types of evolution-based collective intelligence, such as genetic algorithms including: random search in choice sets (search space) and population of individuals, but also differs from them since each individual can learn from itself and others to optimize its performance. When a particle locates a momentary best position (highest fitness value so fare), it shares the information with the other swarm members. As a result, all other swarm members change their positions to the direction of the target. The track and the velocity of a particle are defined individually and depend on its own experience and the experience of the most effective member of the swarm [3].

The application of PSO in the field of energy engineering is widespread. Al-Saedi et al. [4] elaborated an optimal power control strategy, for an inverter based Distributed Generation unit, in an autonomous microgrid operation based on real-time self-tuning method using PSO. Clarke et al. [5] used PSO to find the trade-off between specific work output and specific heat exchanger area of a binary geothermal power plant. To increase variety during optimum search Zafar et al. [6] applied fully informed PSO to reduce loss in power transmission. In order to compensate the instability of differential evolution and early convergence of PSO, Gnanambal et al. [7] uses hybridized DE-PSO algorithm to determine the maximum loadability limit of a power system. Ji et al. [8] combined PSO with gravitational search algorithm to solve economic emission load dispatch problems considering various practical constraints. Also for economic load dispatch Hosseinnezhad et al. [9] proposed a Species-based Quantum PSO where the number of groups in any iteration is determined considering the Hamming distance from the seed species to its border. Eslami et al. [10] proposed passive congregation PSO with chaotic sequence inertial weight to find optimal tuning and placement of power system stabilizer. Mariani et al. [11] presented a cost optimal shell and tube heat exchanger design using chaotic quantum-behaved PSO.

A great number of issues are solved with PSO in which the algorithm has been found to be robust, flexible, and stable. It is insensitive to local optimum or saddle and suitable to solve complex optimization problems with many parameters. PSO is fast in solving non-linear, non-differentiable multi-modal problems [12] and it does not require gradient computation. As literature shows conventional PSO is often modified to maintain diversity and avoid premature convergence even if the properties of search space do not justify an altered balance between variety and convergence speed. Complex engineering problems, where the evaluation of a single particle requires significant computational effort, diversity could cause major running time. The aim of this article is to demonstrate how conventional PSO outperforms a modified PSO when energy conversion system is optimized from thermodynamic viewpoint involving powerful plant performance monitoring software.

# 2 The PSO concept

Consider an unconstrained *D*-dimensional minimization problem as follow:

$$Min f(X), X = \left[x^1, \dots x^j, \dots x^D\right]$$
(1)

where *X*, as a member of the swarm is a solution to be optimized in a form of a *D*-dimensional vector. Assumed that  $x_i^j$  is the position and  $v_i^j$  is the velocity of the *i*th particle on the *j*th dimension their values can be updated by iteration as follows [13]:

$$v_i^j = v_i^j + c_1 \cdot r 1_i^j \cdot \left( pbest_i^j - x_i^j \right) + c_2 \cdot r 2_i^j \cdot \left( gbest_i^j - x_i^j \right),$$

$$(2)$$

$$x_i^j = x_i^j + v_i^j \cdot \Delta t, \qquad (3)$$

where  $X_i = (x_i^1 ... x_i^j ... x_i^D)$  and  $V_i = (v_i^1 ... v_i^j ... v_i^D)$  represents the position and velocity, respectively of the *i*th particle in the *D*-dimensional search space while  $pbest_i = (pbest_i^1 ... pbest_i^J)$  and  $gbest_i = (gbest_i^1 ... gbest_i^J)$  represents the best position of the *i*th particle and the overall best position of the swarm discovered so fare.  $\Delta t$  refers to the time steps between two iterations and can be considered as 1. The acceleration constants cI and c2 are the cognitive and social learning rates, respectively, denoting the relative importance of *pbest* and *gbest* positions.  $r1_i^j$  and  $r2_i^j$  are randomly generated numbers in the range [0,1].

Since its introduction many researchers have worked on improving the performance of PSO by modifying the velocity updating strategy of the original algorithm. The ratio of global and local exploration of new areas depends on the quality and quantity of the elite examples who share their information with neighbors. In this paper single elite and multiple elite algorithms are tested.

In Canonical PSO (CPSO) [12] only the best particle shares information with neighbors. Its velocity updating differs from the original algorithm in the use of inertia weight w alone, which keep balance between global and local search abilities:

$$v_i^j = w_i \cdot v_i^j + c_1 \cdot r 1_i^j \cdot \left( pbest_i^j - x_i^j \right) + c_2 \cdot r 2_i^j \cdot \left( gbest_i^j - x_i^j \right).$$

$$(4)$$

Although several variants of inertia weight are proposed the one applied in canonical form is linearly descending  $w_i = w_{max} - [(w_{max} - w_{min}) / i_{max}] \times i)$ .

Comprehensive Learning Strategy PSO (CLPSO) [14] applies multiple elite examples to prevent premature convergence. The velocity update algorithm of CLPSO is presented in Eq. (5):

$$v_i^j = w_i \cdot v_i^j + c_1 \cdot r \mathbf{1}_i^j \cdot \left( pbest_{fi(j)}^j - x_i^j \right), \tag{5}$$

where  $f_i = (f_i(1) \dots f_i(j) \dots f_i(D))$  defines which neighbors' *pbest* the particle *i* should follow.  $pbest_{f_i(j)}^j$  can be the corresponding dimension of any particle's *pbest* including its own *pbest*. It always depends on a probability factor called *Pc* learning probability:

$$Pc_{i} = 0,05 + 0,45 \cdot \frac{\left(\exp\left(\frac{10(i-1)}{ps-1}\right) - 1\right)}{\exp(10) - 1}.$$
(6)

Besides  $v_{max}^{j}$  maximum velocity has to be given for both algorithms to determine constraints:

$$v_i^j = \min\left(v_{\max}^j, \max\left(v_{\min}^j, v_i^j\right)\right). \tag{7}$$

#### 3 Case study

Previously introduced algorithms are tested on the thermodynamic model of a LANG-BBC 215 MW steam turbine (Fig. 1) to determine highest system efficiency  $(\eta_0)$  under different constraints. These units were operating in Dunamenti Power Plant and Tisza II Thermal Power Plant between the 70's and 90's. The superheated steam is generated by superheater SH of boiler, it next expands in high pressure turbine HPST, it then reheated in reheater RH, and expands first in intermediate pressure turbine IPST than in low pressure turbine LPST to condenser pressure. In the main condenser MC steam condensates at constant pressure and saturation temperature. Feedwater than delivered to the regenerative system by the pump EP. The regenerative system composed of 3 low pressure feedwater heaters E1..E3 and 3 high pressure ones E5..E7 separated by DEA deaerator and a main feedwater pump. MFP is driven by an auxiliary turbine PT where extraction steam expands to condenser pressure. After condensation in auxiliary condenser

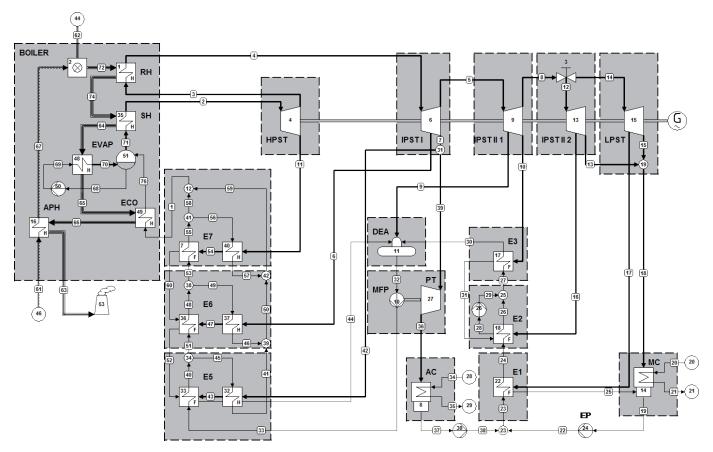


Fig. 1 Simplified scheme of the LANG-BBC 215 MW steam turbine cycle

AC feedwater delivered to low pressure heater E1 by pump. Drains from heater E3 are cascaded to heater E2 and delivered to cold side of E3 by drain pump. Drains from E1 are directed to the condenser. The high pressure feedwater heaters with external desuperheaters and drain coolers have Nekolny-Ricard arrangement. State properties corresponding to Fig. 1 are given in Table 4.

Experience shows that system efficiencies are unimodal functions of the variables [15] which means that a local optimum is also a global one. In most cases, the efficiency function is a very flat function of the variables in the neighborhood of the optimum. Although the search space representing all theoretically possible parameter set is greater than the set of physically possible solutions and in complicated systems the variables are often badly scaled, with properly chosen constraints discontinuities of optimization landscape can be avoided. If however - independently from parameter set – simulation does not converge it causes discontinuities in search space and verify the use of heuristic search algorithms. Fig. 2 shows system efficiency of the steam turbine as the functions of  $p_3$  and  $p_6$  extraction pressures.

This optimization landscape has more discontinuities which are not indicated with iteration number (Fig. 3).

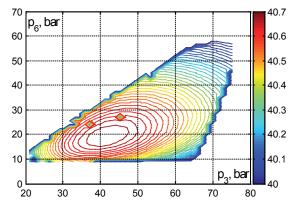


Fig. 2 2-dim search space of LANG-BBC 215 MW steam turbine

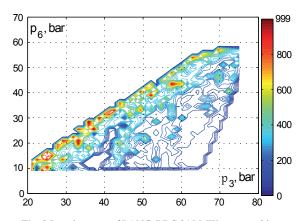


Fig. 3 Iteration map of LANG-BBC 215 MW steam turbine

Design parameters representing dimensions of search space are as follows: live steam parameters, isentropic efficiency and extraction pressures of steam turbine, terminal temperature differences (TTD) and drain cooler approaches (DCA) of feedwater heaters. This way parameter sets contains variables with significant and insignificant effects on system efficiency as well. Also, some of the variables have no optima and have to fall on either the lower or upper limit of search space.

CPSO and CLPSO were tested on a small and a large search space (Table 1) to see how ratio of calculable and incalculable solutions affects the algorithms.

Range	wide	(R1)	narro	w (R2)
Bound	lower	upper	lower	upper
Т <sub>2</sub> , °С	440	580	520	580
η, 1	0,78	0,9	0,84	0,9
p <sub>2</sub> , bar	130	170	150	170
p <sub>11</sub> , bar	25	80	35	45
p <sub>6</sub> , bar	10	40	15	25
p <sub>7</sub> , bar	5	20	6	10
p <sub>9</sub> , bar	2	10	3	5
p <sub>10</sub> , bar	1	5	1	2
p <sub>16</sub> , bar	0,4	2	0,5	0,8
p <sub>17</sub> , bar	0,1	0,8	0,1	0,3
TTD <sub>E1</sub> , °C	2	15	2	8
TTD <sub>E2</sub> , °C	2	15	2	8
TTD <sub>E3</sub> , °C	2	15	2	8
DCA <sub>E3</sub> , °C	2	15	2	8
TTD <sub>E5</sub> , °C	2	15	2	8
DCA <sub>E5</sub> , °C	2	15	2	8
TTD <sub>E6</sub> , °C	2	15	2	8
DCA <sub>E6</sub> , °C	2	15	2	8
TTD <sub>E7</sub> , °C	2	15	2	8
DCA <sub>E7</sub> , °C	2	15	2	8

Parameters of CPSO and CLPSO are set according to [12] and [14] respectively. Number of particles, number of iterations, initial  $(w_{max})$  and final  $(w_{min})$  inertia weights for both algorithms are 25, 120, 0,9 and 0,4 respectively. Cognitive (c1) and social (c2) learning rates of CPSO are 1, learning probability factor (c) of CLPSO is 1,49445, refreshing gap (m) is 7.

Thermodynamic analysis of the optimization process is carried out in GateCycle (GC) plant performance monitoring software using JANAF data for the properties of ideal gases and IAPWS-IF97 for the properties of water and steam. PSO algorithms are developed and all optimization runs are controlled in MATLAB however dynamic data exchange is performed via Microsoft EXCEL. Following steps are performed at each iteration:

Step 1. PSO provides new design variables for GC;

*Step 2.* after simulation with new variables, GC provides thermodynamic properties for PSO search algorithms;

*Step 3.* based on new thermodynamic data, PSO evaluates the objective function and based on results creates new design variables.

#### 4 Results

Performance of swarm intelligences were compared based on different constraints shortlisted in Table 2.

Table 2 Constraints of runs									
Туре	P1	P2	Р3	P4	P5	P6			
Algorithm		CPSO		CLPSO					
Range	R1	R1	R2	R1	R1	R2			
$v_i^j / v_{\rm lim}^j$	0,33	0,166	0,33	0,33	0,166	0,33			

Live steam parameters  $(p_2, T_2)$  and isentropic efficiency  $(\eta)$  have no optima therefore in optimal conditions they reach the upper limit of search space and for the same reason TTDs and DCAs reach the lower one. Since optimal extraction conditions – if stage efficiency is constant - can be estimated either by keeping the temperature change of feedwater heaters constant  $(\Delta T_{FWH,i} = \Delta T_{FWH}^{\Sigma}/n)$  Tor by keeping the rate of temperature change constant  $(q_i = \sqrt[n]{T_{FWH n,out}}/T_{FWH 1,out})$  both methods were calculated and compared with results of PSO based optimum search. All simulations were repeated at least 5 times. Table 3 contains the best results of simulations under different conditions.

Results show that regardless of the size of search space or velocity constraints, CPSO outperforms CLPSO. It provides better results than  $\Delta T_{FWH,i}$  and exceeds  $q_i$  method under P3 condition. CLPSO only surpass  $\Delta T_{FWH,i}$  under P6 condition and does not exceed  $q_i$ . Because of high diversity, multiple elite dependent CLPSO requires significantly more iterations for a successful run than single elite dependent CPSO and have more non-convergent solutions per iteration as well. Since total computation time exceeded 2200 hours (Intel Core 2 Duo E8500, 4GB RAM) iteration threshold was not increased. Both PSOs had their best results in small search spaces (P3, P6).

Figure 4 and Figure 5 shows minimum, maximum, and mean values for system efficiencies ( $\eta_0$ ) and for average number of non-convergent solutions per iteration (ANCS) under different conditions.

Table 3 Results of simulations under different constraints

	$\Delta T_{FWH, i}$	$q_i$	P1	P2	Р3	P4	Р5	P6
$\eta_{o}$ , 1	42,886	42,934	42,934	42,930	42,958	42,859	42,442	42,903
Т <sub>2</sub> , °С	580	580	580	580	580	580	580	580
η, 1	0,9	0,9	0,9	0,9	0,9	0,9	0,9	0,9
p <sub>2</sub> , bar	170	170	170	170	170	170	163,013	170
p <sub>11</sub> , bar	45,798	45,798	43,448	44,039	45,798	51,565	45,780	41,164
p <sub>6</sub> , bar	29,313	24,923	20,938	22,021	22,222	24,975	21,358	20,792
p <sub>7</sub> , bar	15,219	11,156	9,999	10,285	11,046	14,697	13,163	10
p <sub>9</sub> , bar	6,731	4,365	3	4,218	4,289	7,459	6,737	3,600
p <sub>10</sub> , bar	2,851	1,725	1,492	1,857	1,901	2,792	3,778	1,568
p <sub>16</sub> , bar	0,942	0,573	0,5	0,716	0,644	0,896	1,495	0,527
p <sub>17</sub> , bar	0,246	0,172	0,129	0,159	0,149	0,208	0,418	0,185
TTD <sub>E1</sub> , °C	2	2	2	2	2	2	7,442	2,429
TTD <sub>E2</sub> , °C	2	2	2	2	2	2	8,395	2,125
TTD <sub>E3</sub> , °C	2	2	2	2	2	2,792	9,530	2,472
DCA <sub>E3</sub> , °C	2	2	2	11,147	2,002	2	8,805	2
TTD <sub>E5</sub> , °C	2	2	2	2	2	2,999	4,781	2,257
DCA <sub>E5</sub> , °C	2	2	2	15	2	2,071	5,801	3,007
TTD <sub>E6</sub> , °C	2	2	2	2	2	4,258	9,540	3,274
DCA <sub>E6</sub> , °C	2	2	8	2	2	9,121	5,967	2
TTD <sub>E7</sub> , °C	2	2	2	2	2	2	11,236	5,232
DCA <sub>F7</sub> , °C	2	2	6,737	15	2	11,256	14,603	5,805

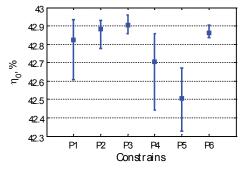


Fig. 4 System efficiencies under different constraints

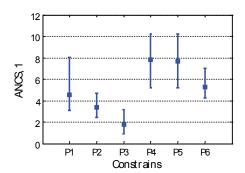


Fig. 5 Average number of non-convergent solutions under different constraints

In a fixed search space, reduced velocity increases the search efficiency of conventional PSO, decreases standard deviation and the number of non-convergent solutions per iteration. Experience shows however that too small velocity maximum decreases global search ability and increases iteration. Wellchosen parameter sets and constraints could increase the effectiveness of the algorithm and reduce the average number of non-convergent solutions per iteration.

Since under given iteration threshold CLPSO did not converged, results of algorithm cannot be assessed. Also, high diversity in velocity updating increases the number of nonconvergent solutions (Fig. 6, Fig. 7). As evaluation time of a particle depends on the number of internal iterations of simulation software which is always higher when particles do not converge, average computational time for CLPSO is higher than for CPSO.

Table 4 Flow properties of LANG-BBC 215 MW steam turbine for base case

	m, kg/s	p, kPa	Т, К	h, kJ/kg	s, kJ/kg-K		m, kg/s	p, kPa	Т, К	h, kJ/kg	s, kJ/kg-K
1	178,6	16188,0	524,6	1093,0	2,778	33	178,6	16188,0	425,0	649,8	1,843
2	178,6	16188,0	813,2	3410,0	6,442	34	638,9	200,0	285,1	50,6	0,181
3	163,6	3844,2	606,5	3055,1	6,539	35	638,9	200,0	291,1	75,3	0,266
4	163,6	3844,2	813,2	3538,9	7,227	36	7,2	4,0	302,1	2317,1	7,690
5	139,6	895,3	618,6	3150,6	7,341	37	7,2	4,0	302,1	121,4	0,422
6	11,1	1844,6	711,8	3335,2	7,291	38	7,2	1373,0	302,2	123,0	0,423
7	13,0	895,3	618,6	3150,6	7,341	39	7,2	895,3	618,6	3150,6	7,341
8	125,0	153,0	438,5	2803,6	7,483	40	178,6	16188,0	444,0	731,5	2,031
9	8,6	430,5	539,6	2997,4	7,409	41	4,6	16188,0	543,9	1186,3	2,953
10	6,0	153,0	438,5	2803,6	7,483	42	5,8	895,3	618,6	3150,6	7,341
11	15,0	3844,2	606,5	3055,1	6,539	43	5,8	895,3	453,8	2787,3	6,655
12	45,2	153,0	438,5	2803,6	7,483	44	31,9	895,3	431,7	669,3	1,927
13	38,4	3,9	301,7	2354,9	7,825	45	4,6	16188,0	444,0	731,5	2,031
14	79,7	153,0	438,5	2803,6	7,483	46	10,8	16188,0	568,0	1309,2	3,174
15	73,8	3,9	301,7	2352,8	7,819	47	11,1	1844,6	526,7	2918,7	6,612
16	6,9	63,2	368,4	2671,2	7,558	48	174,0	16188,0	478,1	880,5	2,354
17	5,9	16,7	329,3	2496,5	7,650	49	10,8	16188,0	478,1	880,5	2,354
18	112,2	3,9	301,7	2353,5	7,821	50	15,4	16188,0	560,9	1272,3	3,109
19	118,1	3,9	301,7	119,7	0,417	51	174,0	16188,0	444,0	731,5	2,031
20	10007,7	200,0	288,1	63,2	0,224	52	26,1	1844,6	452,5	760,8	2,132
21	10007,7	200,0	294,2	88,3	0,311	53	163,3	16188,0	478,1	880,5	2,354
22	118,1	1373,0	301,8	121,3	0,418	54	15,0	3844,2	540,9	2871,3	6,218
23	125,3	1373,0	301,8	121,4	0,418	55	163,3	16188,0	517,5	1059,4	2,714
24	125,3	1373,0	325,9	222,0	0,739	56	10,8	16188,0	517,5	1059,4	2,714
25	5,9	16,7	329,3	235,2	0,783	57	10,8	16188,0	568,2	1310,7	3,177
26	125,3	1373,0	356,2	348,8	1,110	58	152,5	16188,0	517,5	1059,4	2,714
27	138,2	1373,0	356,6	350,5	1,115	59	26,2	16188,0	564,0	1288,2	3,137
28	12,9	63,2	360,4	365,4	1,161	60	15,0	3844,2	483,0	897,7	2,420
29	12,9	1373,0	360,5	367,0	1,161	61	200,0	101,3	288,1	-0,6	6,869
30	138,2	1373,0	381,5	455,4	1,400	62	11,1	300,0	288,1	-1,1	10,172
31	6,0	153,0	362,9	376,0	1,190	63	211,1	101,2	429,0	155,4	7,586
32	178,6	430,5	419,4	616,2	1,804						

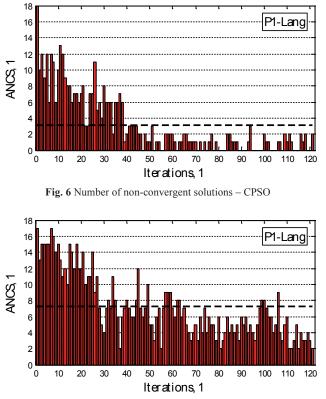


Fig. 7 Number of non-convergent solutions - CLPSO

# **5** Conclusion

PSO is suitable to optimize thermodynamic models of energy conversion systems. Sensitivity of the algorithm to discontinuities of optimization landscape depends on the velocity update algorithm, the size of the velocity relative to search space and the ratio of calculable and incalculable parameter sets. For a fixed search space, reduced velocity increases the search efficiency of conventional PSO, decreases standard deviation and the number of non-convergent solutions per iteration. Small velocity maximum however decreases global search ability and increases iteration. Well-chosen parameter sets and constraints could increase the efficiency of the algorithm and reduce the average number of non-convergent solutions per iteration. Because of high diversity, multiple elite dependent CLPSO requires significantly more iterations for a successful run than single elite dependent CPSO and have more non-convergent solutions per iteration as well. Due to high computational time CLPSO is less suitable for power plant optimization if thermodynamic model is developed in a plant performance monitoring software. Computation time is affected only slightly by iteration threshold and swarm size but is significantly affected by the quality of the variables. This is primarily due to the fact that evaluation time of a particle depends on the number of internal iterations of simulation software, which is always higher when particles do not converge.

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